

$\text{rank}_y/s_1 \leq \text{rank}_x/s_1$