

Visitors Unchained

Using **visitors**
to traverse **abstract syntax with binding**

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The problem

Manipulating abstract syntax with binding requires many standard operations:

- ▶ “**opening**” and “**closing**” binders (in the locally nameless representation);
- ▶ **shifting** (in de Bruijn’s representation);
- ▶ deciding **α -equivalence**;
- ▶ testing whether a name **occurs** free in a term;
- ▶ performing capture-avoiding **substitution**;
- ▶ **converting** user-supplied terms to the desired internal representation;
- ▶ etc., etc.

This requires a lot of **boilerplate**, a.k.a. **nameplate** (Cheney).

Isn't this a solved problem?

It may well be, depending on your programming language of choice.

Haskell has

- ▶ FreshLib (Cheney, 2005),
- ▶ Unbound (Weirich, Yorgey, Sheard, 2011),
- ▶ Bound (Kmett, 2013?),
- ▶ maybe more?

These libraries may have bad performance, though (?).

OCaml has... not much.

- ▶ *Caml* (F.P., 2005) is monolithic, inflexible, and has performance issues, too.

(The problem also arises in theorem provers. Not studied here.)

Goal

I wish to **scrap my nameplate**, in **OCaml**, in a manner that is

- ▶ as **modular**, open-ended, **customizable** as possible,
- ▶ while relying on **as little code generation** as possible,
- ▶ while (simultaneously!) supporting **multiple representations** of names,
- ▶ and supporting **multiple binding constructs**, possibly user-defined.

It turns out that this can be done by exploiting the “**visitor**” design pattern.

Visitors



Installation & configuration

Installation:

```
opam update
opam install visitors
```

To configure ocamlbuild, add this in `_tags`:

```
true: \
  package(visitors.ppx), \
  package(visitors.runtime)
```

To configure Merlin, add this in `.merlin`:

```
PKG visitors.ppx
PKG visitors.runtime
```

An “iter” visitor

Annotating a type definition with `[@@deriving visitors { ... }]`...

```
type expr =  
  | EConst of int  
  | EAdd of expr * expr  
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  method visit_EAdd env c0 c1 =  
    let r0 = self#visit_expr env c0 in  
    let r1 = self#visit_expr env c1 in  
    ()  
  method visit_expr env this =  
    match this with  
    | EConst c0 ->  
      self#visit_EConst env c0  
    | EAdd (c0, c1) ->  
      self#visit_EAdd env c0 c1  
end
```

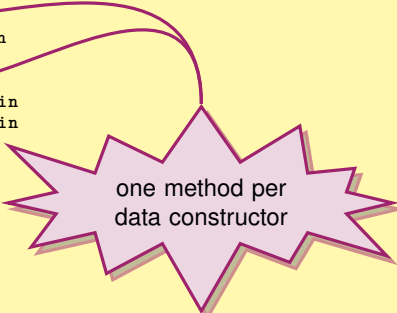
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one method per
data constructor


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one method per
data type

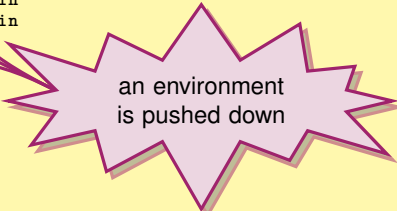
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    match this with  
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      self#visit_EConst env c0  
    | EAdd (c0, c1) ->  
      self#visit_EAdd env c0 c1  
end
```



an environment
is pushed down

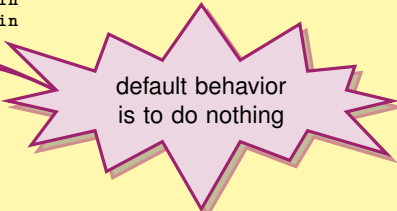
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    let r1 = self#visit_expr env c1 in  
    ()  
  method visit_expr env this =  
    match this with  
    | EConst c0 ->  
      self#visit_EConst env c0  
    | EAdd (c0, c1) ->  
      self#visit_EAdd env c0 c1  
end
```



default behavior
is to do nothing

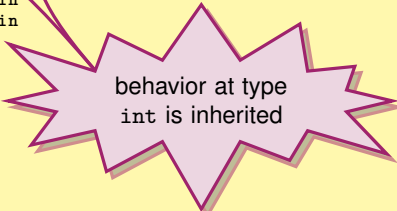
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    ()  
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      self#visit_EConst env c0  
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      self#visit_EAdd env c0 c1  
end
```



behavior at type
int is inherited

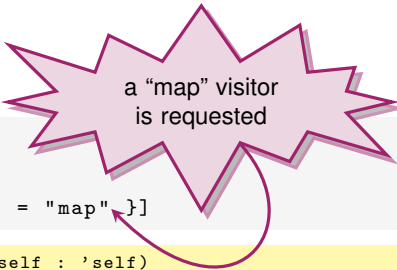
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A “map” visitor

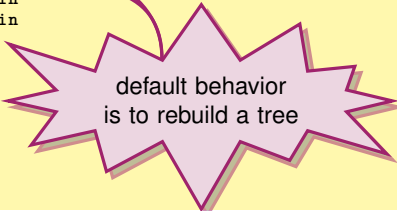
There are several varieties of visitors:

```
type expr =  
  | EConst of int  
  | EAdd of expr * expr  
  [@@deriving visitors { variety = "map" }]
```

```
class virtual ['self] map = object (self : 'self)  
  inherit [_] VisitorsRuntime.map  
  method visit_EConst env c0 =  
    let r0 = self#visit_int env c0 in  
    EConst r0  
  method visit_EAdd env c0 c1 =  
    let r0 = self#visit_expr env c0 in  
    let r1 = self#visit_expr env c1 in  
    EAdd (r0, r1)  
  method visit_expr env this =  
    match this with  
    | EConst c0 ->  
      self#visit_EConst env c0  
    | EAdd (c0, c1) ->  
      self#visit_EAdd env c0 c1  
end
```



a “map” visitor
is requested



default behavior
is to rebuild a tree

Using a “map” visitor

Inherit a visitor class and **override** one or more methods:

```
let add e1 e2 =      (* A smart constructor. *)
  match e1, e2 with
  | EConst 0, e
  | e, EConst 0 -> e
  | _, _ ->         EAdd (e1, e2)

let optimize : expr -> expr =
  let v = object (self)
    inherit [_] map
    method! visit_EAdd env e1 e2 =
      add
        (self#visit_expr env e1)
        (self#visit_expr env e2)
  end in
  v # visit_expr ()
```

This addition-optimization pass is **unchanged** if more expression forms are added.

What we have seen so far

- ▶ **Several built-in varieties:** `iter`, `map`, ...
- ▶ **Arity two**, too: `iter2`, `map2`, ...
- ▶ Generated visitor methods are **monomorphic** (in this talk),
- ▶ and their types are **inferred**.
- ▶ Visitor classes are nevertheless **polymorphic**.
- ▶ **Polymorphic** visitor methods can be hand-written and inherited.

Support for parameterized data types

Visitors can traverse parameterized data types, too.

- ▶ But: how does one traverse a subtree of type 'a?

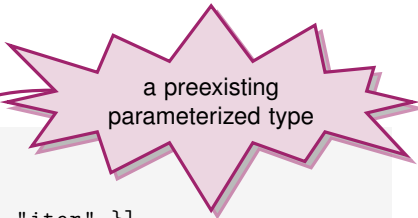
Two approaches are supported:

- ▶ declare a **virtual visitor method** `visit_'a`
- ▶ pass a **function** `visit_'a` to every visitor method.
 - ▶ allows / requires methods to be polymorphic in 'a
 - ▶ more compositional

In this talk: a bit of both (details omitted...).

Visiting preexisting types

Lists can be visited, too.



a preexisting
parameterized type

```
type expr =  
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  | EAdd of expr list  
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```

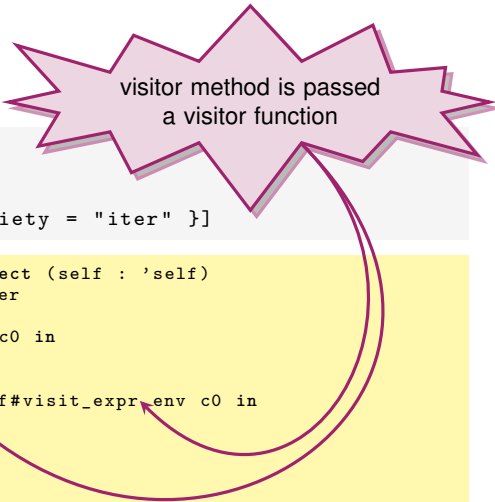
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    let r0 = self#visit_list self#visit_expr env c0 in  
    ()  
  method visit_expr env this =  
    match this with  
    | EConst c0 ->  
      self#visit_EConst env c0  
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end
```

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    let r0 = self#visit_list self#visit_expr env c0 in  
    ()  
  method visit_expr env this =  
    match this with  
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      self#visit_EConst env c0  
    | EAdd c0 ->  
      self#visit_EAdd env c0  
end
```



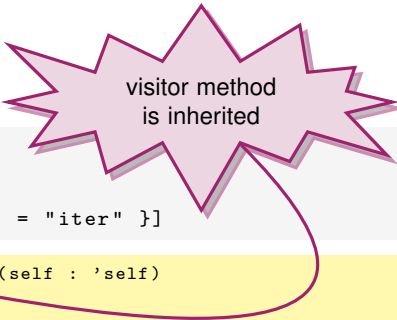
visitor method is passed
a visitor function

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    ()  
  method visit_expr env this =  
    match this with  
    | EConst c0 ->  
      self#visit_EConst env c0  
    | EAdd c0 ->  
      self#visit_EAdd env c0  
end
```



visitor method
is inherited

Predefined visitor methods

The class `VisitorsRuntime.map` offers this method:

```
class ['self] map = object (self)
  (* One of many predefined methods: *)
  method private visit_list: 'env 'a 'b .
    ('env -> 'a -> 'b) -> 'env -> 'a list -> 'b list
  = fun f env xs ->
    match xs with
    | [] ->
      []
    | x :: xs ->
      let x = f env x in
      x :: self # visit_list f env xs
end
```

This method is **polymorphic**, so multiple instances of `list` are not a problem.

Visitors – a summary



Although they follow fixed patterns, visitors are quite **versatile**.

They are like higher-order functions, only more **customizable** and **composable**.

More fun with visitors:

- ▶ visitors for **open data types** and their fixed points ([link](#));
- ▶ visitors for **hash-consed data structures** ([link](#));
- ▶ **iterators** out of visitors ([link](#)).

In the remainder of this talk:

- ▶ Can we traverse **abstract syntax with binding**?

Visitors Unchained



Dealing with binding

Can a visitor traverse **abstract syntax with binding** constructs?

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Can this be done in a **modular** way?

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Exactly which **separation of concerns** should one enforce?

Dealing with binding

Can a visitor traverse **abstract syntax with binding** constructs?

Can this be done in a **modular** way?

Exactly which **separation of concerns** should one enforce?

- ▶ There are many **binding constructs**,
 - ▶ there are even **combinator languages** for describing binding structure!
- ▶ and many common **operations** on terms,
 - ▶ often specific of one **representation** of names and binders,
 - ▶ sometimes specific of **two** such representations, e.g., **conversions**.
- ▶ Can we insulate the **end user** from this complexity?

We suggest distinguishing **three** principals...



end
user



A black and white photograph of three men in Western-style clothing. The man in the center is wearing a cowboy hat, sunglasses, and a scarf. The man on the left is wearing a suit and tie. The man on the right is wearing a bowler hat and holding a revolver. The background is white with a red splatter effect. Two orange starburst shapes with red outlines contain the text 'end user' and 'operations specialist'.

end
user

operations
specialist

A black and white photograph of three men in Western-style clothing, including hats and scarves. The background is white with red splatters. Three orange starburst shapes with red outlines are overlaid on the image, each containing text. The man on the left is looking slightly to the right. The man in the center is wearing a wide-brimmed hat and sunglasses. The man on the right is wearing a bowler hat and holding a rifle.

end
user

binder
maestro

operations
specialist

The end user



Desiderata

The end user wishes:

- ▶ to describe the structure of ASTs in a concise and **declarative** style,
- ▶ not to be bothered with implementation details,
- ▶ possibly to have access to **several representations** of names,
- ▶ to get access to a toolkit of **ready-made operations** on terms.

Example: abstract syntax of the λ -calculus

Let the type `('bn, 'term) abs` be a synonym for `'bn * 'term`.

The end user defines his syntax as follows:

```
type ('bn, 'fn) term =
  | TVar of 'fn
  | TLambda of ('bn, ('bn, 'fn) term) abs
  | TApp of ('bn, 'fn) term * ('bn, 'fn) term
[@@deriving visitors { variety = "map";
                      ancestors = ["BindingForms.map"] }]
type raw_term      = (string, string) term
type nominal_term  = (Atom.t, Atom.t) term
type debruijn_term = (unit,      int) term
```

He gets **multiple representations** of names.

- ▶ At least two are used in any single application. (Parsing. Printing.)


He gets **visitors** for free. The method `visit_abs` is used at abstractions.

- ▶ `iter`, `map`, `iter2` needed in practice. Focusing on `map` in this talk.

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provided by the binder maestro

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The binder maestro



An easy job?

Implementing `visit_abs` is the task of our sophisticated binder maestro.

The key is to **extend the environment** when entering the scope of a binder.

Easy?

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The key is to **extend the environment** when entering the scope of a binder.

Easy? Maybe — yet, the binder maestro:

- ▶ does not know **what operation** is being performed,
- ▶ does not know **what representation(s)** of names are in use,
- ▶ therefore does not know the types of names and environments,
- ▶ let alone **how** to extend the environment.

What he knows is **where** and **with what names** to extend the environment.

A convention

The binder maestro agrees on a **deal** with the operations specialist.

"I tell you when to extend the environment; you do the dirty work."

The binder maestro **calls** a method which the operations specialist **provides**:

```
(* A hook that defines how to extend the environment. *)  
method private virtual extend: 'env -> 'bn1 -> 'env * 'bn2
```

This is a bare-bones **API** for describing binding constructs.

Visiting an abstraction

The class `BindingForms.map` offers the method `visit_abs`:

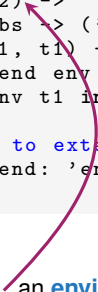
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class virtual ['self] map = object (self : 'self)
  (* A visitor method for the type abs. *)
  method private visit_abs: 'term1 'term2 . _ ->
    ('env -> 'term1 -> 'term2) ->
    'env -> ('bn1, 'term1) abs -> ('bn2, 'term2) abs
  = fun _ visit_'term env (x1, t1) ->
    let env, x2 = self#extend env x1 in
    let t2 = visit_'term env t1 in
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This method:

- ▶ takes a **visitor function** for terms, an **environment**,
- ▶ an abstraction, i.e., a **pair** of a name and a term, and
- ▶ returns a pair of a **transformed name** and a **transformed term**.

Visiting an abstraction

That's **all there is** to single-name abstractions.

More binding constructs later on...

For now, let's turn to the final participant.

The operations specialist



A toolbox of operations

There are many operations on terms that the end user might wish for:

- ▶ testing terms for **equality** up to α -equivalence,
- ▶ finding out which names are **free** or **bound** in a term,
- ▶ applying a **renaming** or a **substitution** to a term,
- ▶ **converting** a term from one representation to another,
- ▶ (plus application-specific operations.)

Implementing an operation

To implement one operation, the specialist decides:

- ▶ the **types** of names and environments,
- ▶ **what to do** at a **free name** occurrence,
- ▶ **how to extend** the environment when entering the scope of a **bound name**.

Implementing `import`

As an example, let's implement `import`, which converts raw terms to nominal terms.

1. An import environment maps strings to atoms:

```
module StringMap = Map.Make(String)
type env = Atom.t StringMap.t
let empty : env = StringMap.empty
```

Implementing `import`

2. When the scope of x is entered, the environment is extended with a mapping of the string x to a fresh atom a .

```
let extend (env : env) (x : string) : env * Atom.t =  
  let a = Atom.fresh x in  
  let env = StringMap.add x a env in  
  env, a
```

(An **atom** carries a unique integer identity.)

This is true regardless of which binding constructs are traversed.

Implementing `import`

3. When an occurrence of the string `x` is found, the environment is looked up so as to find the corresponding atom.

```
exception Unbound of string
let lookup (env : env) (x : string) : Atom.t =
  try StringMap.find x env
  with Not_found -> raise (Unbound x)
```

Implementing `import`

The previous instructions are grouped in a little class — a “kit”:

```
class ['self] map = object (_ : 'self)
  method private extend      = extend
  method private visit_'fn = lookup
end
```

This is `KitImport.map`.

That's all there is to it... **but...**

Gluey business



The end user must **work** a little bit to **glue** everything together...

For each operation, the end user must write 5 lines of glue code:

```
let import_term env t =
  (object
    inherit [_] map           (* generated by visitors *)
    inherit [_] KitImport.map (* provided by AlphaLib *)
  end) # visit_term env t
```

For 15 operations, this hurts.

Functors can help in simple cases, but are not flexible enough.

C-like **macros** help, but are ugly. Is there a better way?

Towards advanced binding constructs



Defining new binding constructs

There are **many binding constructs** out there.

- ▶ “let”, “let rec”, patterns, telescopes, ...

We have seen how to **programmatically** define a binding construct.

Can it be done in a more **declarative** manner?

A domain-specific language

Here is a little language of **binding combinators**:

t	$::=$...	sums, products, free occurrences of names, etc.
		$\text{abstraction}(p)$	a pattern, with embedded subterms
p	$::=$...	sums, products, etc.
		$\text{binder}(x)$	a binding occurrence of a name
		$\text{outer}(t)$	an embedded term
		$\text{rebind}(p)$	a pattern in the scope of any bound names on the left

Inspired by $C\alpha\text{ml}$ (F.P., 2005) and Unbound (Weirich et al., 2011).

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A domain-specific language

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t	::=	...	sums, products, free occurrences of names, etc.
		abstraction(p)	a pattern, with embedded subterms
		bind(p, t)	— sugar for abstraction($p \times \text{inner}(t)$)
p	::=	...	sums, products, etc.
		binder(x)	a binding occurrence of a name
		outer(t)	an embedded term
		rebind(p)	a pattern in the scope of any bound names on the left
		inner(t)	— sugar for rebind(outer(t))

Inspired by $C\alpha$ ml (F.P., 2005) and Unbound (Weirich et al., 2011).

Example use: telescopes

A dependently-typed λ -calculus whose Π and λ forms involve a telescope:

```
#define tele      ('bn, 'fn) tele
#define term      ('bn, 'fn) term
(* The types that follow are parametric in 'bn and 'fn: *)

type tele =
  | TeleNil
  | TeleCons of 'bn binder * term outer * tele rebound

and term =
  | TVar of 'fn
  | TPi  of (tele, term) bind
  | TLam of (tele, term) bind
  | TApp of term * term list

[@@deriving visitors {
  variety = "map";
  ancestors = ["BindingCombinators.map"]
}]
```

Implementation

These primitive constructs are just annotations:

```
type 'p abstraction = 'p
type 'bn binder = 'bn
type 't outer = 't
type 'p rebind = 'p
```

Their presence triggers calls to appropriate (hand-written) `visit_` methods.

Implementation

While visiting a pattern, we keep track of:

- ▶ the **outer environment**, which existed outside this pattern;
- ▶ the **current environment**, extended with the bound names encountered so far.

Thus, while visiting a pattern, we use a richer type of **contexts**:

```
type 'env context = { outer: 'env; current: 'env ref }
```

— Not every visitor method need have the same type of environments!

With this in mind, the implementation of the `visit_` methods is straightforward...

Implementation

This code takes place in a map visitor:

```
class virtual ['self] map = object (self : 'self)
  method private virtual extend: 'env -> 'bn1 -> 'env * 'bn2
    (* The four visitor methods are inserted here... *)
end
```

1. At the root of an abstraction, **a fresh context** is allocated:

```
method private visit_abstraction: 'env 'p1 'p2 .
  ('env context -> 'p1 -> 'p2) ->
  'env -> 'p1 abstraction -> 'p2 abstraction
= fun visit_p env p1 ->
  visit_p { outer = env; current = ref env } p1
```

Implementation

2. When a bound name is met, the **current** environment is **extended**:

```
method private visit_binder: _ ->
  'env context -> 'bn1 binder -> 'bn2 binder
= fun visit_'bn ctx x1 ->
  let env = !(ctx.current) in
  let env, x2 = self#extend env x1 in
  ctx.current := env;
  x2
```

Implementation

3. When a term that is **not in the scope** of the abstraction is found, it is visited in the **outer** environment.

```
method private visit_outer: 'env 't1 't2 .
  ('env -> 't1 -> 't2) ->
  'env context -> 't1 outer -> 't2 outer
= fun visit_t ctx t1 ->
  visit_t ctx.outer t1
```


Implementation

4. When a subpattern marked `rebind` is found, the **current** environment is installed as the **outer** environment.

```
method private visit_rebind: 'env 'p1 'p2 .
  ('env context -> 'p1 -> 'p2) ->
  'env context -> 'p1 rebind -> 'p2 rebind
= fun visit_p ctx p1 ->
  visit_p { ctx with outer = !(ctx.current) } p1
```

This affects the meaning of `outer` inside `rebind`.

Conclusion



Conclusion

Visitors are **powerful**.

Visitor classes are **partial**, **composable** descriptions of operations.

Visitors **can** traverse **abstract syntax with binding**.

- ▶ Syntax, binding forms, operations can be **separately** described.
- ▶ Syntax and even binding forms can be described in a **declarative** style.
- ▶ Open-ended, customizable approach.

Limitations:

- ▶ C-like macros are currently required.
- ▶ No proofs.
- ▶ Some operations may not fit the visitor framework;
- ▶ Some binding forms do not easily fit in the low-level framework or in the higher-level DSL, e.g., Unbound's *Rec*.